

ТИПОВОЙ РАСЧЕТ
«Элементарная математика»

Задание 1. Сократить дробь.

$$\text{1.1. } \frac{3x^2 + 5x - 2}{4x^2 + 11x + 6}.$$

$$\text{1.2. } \frac{7x^2 - 2x - 5}{2x^2 - x - 1}.$$

$$\text{1.3. } \frac{3x^2 + 4x + 1}{3x^2 + x - 2}.$$

$$\text{1.4. } \frac{x^2 + 3x - 10}{2x^2 + 11x + 5}.$$

$$\text{1.5. } \frac{2x^2 - 5x - 3}{3x^2 - 10x + 3}.$$

$$\text{1.6. } \frac{2x^2 - 3x + 1}{x^2 + 5x - 6}.$$

$$\text{1.7. } \frac{-2x^2 + 7x - 3}{2x - 1}.$$

$$\text{1.8. } \frac{5 - x}{3x^2 - 13x - 10}.$$

$$\text{1.9. } \frac{4x^2 + 9x + 5}{2x^2 + 5x + 3}.$$

$$\text{1.10. } \frac{4x^2 + 7x + 3}{5x^2 + 11x + 6}.$$

$$\text{1.11. } \frac{3x^2 + 7x + 4}{6x^2 + 11x + 5}.$$

$$\text{1.12. } \frac{2x^2 + 3x - 1}{6x^2 + 7x + 1}.$$

$$\text{1.16. } \frac{5x^2 + 7x + 2}{5x^2 + 6x + 1}.$$

$$\text{1.17. } \frac{2x^2 + x - 3}{-4x^2 - 4x + 3}.$$

$$\text{1.18. } \frac{9x^2 + 3x - 2}{-6x^2 - x + 2}.$$

$$\text{1.19. } \frac{5x^2 + 6x + 1}{-5x^2 + 4x + 1}.$$

$$\text{1.20. } \frac{6x^2 + 7x + 1}{12x^2 + 8x + 1}.$$

$$\text{1.21. } \frac{-2x^2 + x + 1}{6x^2 - 5x - 1}.$$

$$\text{1.22. } \frac{4x^2 - x - 5}{5x^2 + 9x + 4}.$$

$$\text{1.23. } \frac{2x^2 + x - 1}{2x^2 + 3x + 1}.$$

$$\text{1.24. } \frac{5x^2 + 3x - 2}{7x^2 + 8x + 1}.$$

$$\text{1.25. } \frac{6x^2 + 7x + 2}{9x^2 + 3x - 2}.$$

$$\text{1.26. } \frac{5x^2 + 8x + 3}{6x^2 + 7x + 1}.$$

$$\text{1.27. } \frac{2x^2 + 3x + 1}{5x^2 + 9x + 4}.$$

1.13. $\frac{3x^2 + 4x - 4}{-x^2 + 4x + 12}.$

1.14. $\frac{8x^2 + 6x + 1}{2x^2 + 3x + 1}.$

1.15. $\frac{2x^2 + x - 3}{3x^2 + 2x - 5}.$

1.28. $\frac{3x^2 - 2x - 1}{3x^2 + 4x + 1}.$

1.29. $\frac{4x^2 + 5x + 1}{7x^2 + 9x + 2}.$

1.30. $\frac{2x^2 + 5x + 2}{4x^2 + 11x + 6}.$

Задание 2. Выделить полный квадрат.

2.1. а) $x^2 + 12x - 4;$

б) $4x^2 + 4x + 3.$

2.2. а) $x^2 + 6x + 13;$

б) $x^2 + 3x - 1.$

2.3. а) $x^2 + 20x - 14;$

б) $2x^2 - 12x + 3.$

2.4. а) $x^2 + 2x + 7;$

б) $x^2 - x + 5.$

2.5. а) $x^2 - 16x + 36;$

б) $3x^2 + 12x - 7.$

2.6. а) $x^2 + 4x + 1;$

б) $x^2 - 3x + 1.$

2.7. а) $x^2 - 1x + 19;$

б) $2x^2 + 12x - 7.$

2.8. а) $x^2 - 16x + 70;$

б) $x^2 - 3x + 2.$

2.9. а) $x^2 + 20x - 2;$

б) $5x^2 - 30x + 2.$

2.10. а) $x^2 + 2x + 12;$

б) $x^2 + x + 2.$

2.11. а) $x^2 + 6x + 4;$

б) $4x^2 - 4x + 5.$

2.12. а) $x^2 - 14x + 36;$

б) $x^2 - 5x + 1.$

2.13. а) $x^2 - 18x + 45;$

б) $3x^2 - 12x + 2.$

2.14. а) $x^2 + 12x + 16;$

б) $x^2 - x + 4.$

2.15. а) $x^2 - 2x - 4;$

б) $4x^2 + 8x + 7.$

2.16. а) $x^2 - 6x + 2;$

б) $x^2 + 5x + 1.$

2.17. а) $x^2 + 8x + 14;$

б) $5x^2 + 30x - 1.$

2.18. а) $x^2 - 20x + 51;$

б) $x^2 + x + 1.$

2.19. а) $x^2 + 4x + 16;$

б) $2x^2 - 18x + 25.$

- 2.20.** а) $x^2 + 14x + 39$; б) $x^2 - 3x + 7$.
- 2.21.** а) $x^2 - 18x - 12$; б) $4x^2 - 8x + 3$.
- 2.22.** а) $x^2 + 16x + 40$; б) $x^2 + x - 4$.
- 2.23.** а) $x^2 + 10x - 2$; б) $2x^2 - 4x + 5$.
- 2.24.** а) $x^2 - 8x + 19$; б) $x^2 - x - 4$.
- 2.25.** а) $x^2 + 4x - 7$; б) $9x^2 + 36x + 10$.
- 2.26.** а) $x^2 + 18x + 30$; б) $x^2 + 5x - 7$.
- 2.27.** а) $x^2 - 12x + 37$; б) $2x^2 - 8x + 1$.
- 2.28.** а) $x^2 + 14x + 9$; б) $x^2 - 3x + 10$.
- 2.29.** а) $x^2 + 10x + 33$; б) $3x^2 - 12x + 5$.
- 2.30.** а) $x^2 - 8x - 1$; б) $x^2 + 3x - 8$.

Задание 3. Выполнить деление многочлена $P_n(x)$ на $Q_m(x)$.

	$P_n(x)$	$Q_m(x)$
3.1	$2x^7 - x^5 + 6x^4 - 4x^3 - 3x^2 + 2x$	$x^5 + 3x^2 - 2x$
3.2	$3x^5 + 5x^4 - 6x^2 + 5x + 25$	$x^4 - 2x + 5$
3.3	$x^5 - x^4 + 3x^3 - 9x + 6$	$x^4 + 3x - 6$
3.4	$6x^6 + 4x^5 + 3x^4 + 2x^3 - 6x - 4$	$2x^5 + x^3 - 2$
3.5	$2x^7 + 4x^5 + 2x^4 - 7x^3 - 14x - 7$	$x^3 + 2x - 1$
3.6	$6x^6 + 27x^4 + 4x^3 - 10x^2 + 18x + 45$	$2x^2 + 9$
3.7	$9x^7 - 3x^5 - 14x^3 - 4x$	$3x^3 + x$

3.8	$x^6 + 3x^5 - 7x^3 - 21x^2 + 8x + 24$	$x^5 - 7x^2 + 8$
3.9	$5x^9 - 10x^8 + 20x^6 - 2x^3 + 4x^2 - 8$	$x^3 - 2x^2 + 4$
3.10	$8x^9 - 26x^7 - 7x^5 + 6x^4 - 21x^2$	$2x^4 - 7x^2$
3.11	$3x^5 + 2x^4 + x^3 - 21x^2 - 3x + 5$	$x^3 + x^2 - 7$
3.12	$3x^7 - x^6 - 6x^4 + 4x^3 + 6x^2 - 3$	$x^5 - 2x^2 + 2$
3.13	$2x^7 - x^6 + 2x^5 + x^4 + 3x^2$	$x^5 - 3x$
3.14	$x^7 + x^6 - 3x^5 + x^4 + 3x^3 - 3x$	$x^2 + x - 3$
3.15	$x^8 + x^7 - x^5 - 2x^4 + 3x^3 - 3x$	$x^3 + x^2 - 1$
3.16	$4x^5 - 7x^3 + 7x^2 + 6x - 10$	$x^3 - x + 2$
3.17	$4x^6 - 3x^4 + 8x^3 - 5x^2 - 3x - 1$	$x^4 + 2x - 1$
3.18	$4x^5 - 15x^3 + 19x^2 + 12x - 19$	$x^3 - 3x + 5$
3.19	$8x^6 - 6x^4 + 4x^3 - 5x^2 - 1$	$2x^4 + x - 1$
3.20	$8x^5 - 4x^4 - 6x^3 + 10x^2 + 3x - 10$	$2x^3 - x^2 + 2$
3.21	$3x^6 + 4x^4 - 12x^3 - 2x^2 + 3$	$x^3 + 2x - 4$
3.22	$3x^7 - 2x^5 - 3x^4 + 15x^3 + 4x^2 - 18x + 3$	$x^4 - x + 5$
3.23	$3x^8 - 2x^6 - 6x^4 + 9x^3 - 2x^6 - 14x + 3$	$x^5 - 2x + 3$

3.24	$6x^5 - 3x^4 + 11x^3 + 4x^2 - 18x + 3$	$2x^2 - x + 5$
3.25	$9x^6 - 6x^3 - 2x^2 - 4x + 3$	$3x^3 + 2x - 2$
3.26	$6x^6 + 3x^5 - 21x^4 - x^2 + 8x$	$3x^4 - x$
3.27	$4x^7 + 2x^6 - 14x^5 + 2x^4 - 5x^2$	$5x^5 + x^2$
3.28	$2x^7 + x^6 - 7x^5 + 6x^4 + 2x^3 - 15x^2$	$x^5 + 3x^2$
3.29	$6x^6 + 3x^5 - 21x^4 - 4x^3 + 13x + 7$	$3x^4 - 2x$
3.30	$10x^5 + 7x^4 - 35x^3 + 5x^2 - 4$	$5x^3 + x^2$

Задание 4. Решить неравенство.

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|---|---|
| 4.1. $ 3x^2 + 5x - 1 \leq 1.$
4.2. $ 7x^2 + 2x - 3 > 2.$
4.3. $ 2x^2 - x + 3 \geq 4.$
4.4. $ x^2 + 3x - 1 < 9.$
4.5. $ 3x^2 - 10x + 4 > 1.$
4.6. $ 2x^2 - 3x + 6 \leq 5.$
4.7. $ -2x^2 + 7x + 1 \geq 4.$
4.8. $ 3x^2 - 13x - 8 < 2.$
4.9. $ 4x^2 + 9x + 6 < 1.$
4.10. $ 5x^2 + 11x + 9 \geq 3.$
4.11. $ 3x^2 + 7x + 8 \leq 4.$ | 4.16. $ 5x^2 + 6x + 7 > 6.$
4.17. $ -4x^2 - 4x + 5 < 2.$
4.18. $ 9x^2 + 3x + 4 \leq 6.$
4.19. $ 5x^2 + 6x + 5 \geq 4.$
4.20. $ 6x^2 + 7x + 9 > 8.$
4.21. $ -2x^2 + x + 7 < 6.$
4.22. $ 4x^2 - x - 3 \geq 2.$
4.23. $ 6x^2 - 5x + 3 \leq 4.$
4.24. $ 5x^2 + 3x + 2 > 4.$
4.25. $ 9x^2 + 3x + 5 < 7.$
4.26. $ 7x^2 + 8x + 7 \geq 6.$ |
|---|---|

4.12. $|6x^2 + 7x + 6| > 5.$

4.13. $|-x^2 + 4x + 14| < 2.$

4.14. $|2x^2 + 3x + 5| \geq 4.$

4.15. $|3x^2 + 2x - 2| \leq 3.$

4.27. $|2x^2 + 3x + 4| \leq 3.$

4.28. $|-3x^2 + 2x + 6| < 5.$

4.29. $|4x^2 + 5x + 7| > 6.$

4.30. $|-2x^2 + 5x + 7| \geq 4.$

Задание 5. Построить график функции.

5.1. $f(x) = \begin{cases} -x, & x \leq 0 \\ x^2, & 0 < x \leq 1 \\ \ln x + 1, & x > 1 \end{cases}$

5.16. $f(x) = \begin{cases} -3x, & x \leq 1 \\ x^2 - 4, & 1 < x < 3 \\ \frac{3}{x}, & x \geq 3 \end{cases}$

5.2. $f(x) = \begin{cases} -x^2, & x \leq 0 \\ \sin x, & 0 < x < \frac{\pi}{2} \\ 1, & x > \frac{\pi}{2} \end{cases}$

5.17. $f(x) = \begin{cases} 2x + 1, & x < -1 \\ x^2, & -1 \leq x < 2 \\ \frac{-2}{x}, & x > 2 \end{cases}$

5.3. $f(x) = \begin{cases} 2x^2, & x \leq 0 \\ \ln x, & 0 < x \leq 1 \\ \frac{1}{x}, & x > 1 \end{cases}$

5.18. $f(x) = \begin{cases} -x, & x < 0 \\ \sin x, & 0 \leq x < \pi \\ x - \pi, & x \geq \pi \end{cases}$

5.4. $f(x) = \begin{cases} -\frac{4}{x}, & x \leq -4 \\ x + 5, & -4 < x < 1 \\ 4^x, & x \geq 1 \end{cases}$

5.19. $f(x) = \begin{cases} x + 1, & x \leq 0 \\ \cos x, & 0 < x < \frac{\pi}{2} \\ \frac{\pi}{2} - x, & x \geq \frac{\pi}{2} \end{cases}$

5.5. $f(x) = \begin{cases} -2x, & x < -1 \\ x^2 + 1, & -1 \leq x < 2 \\ 2^x, & x \geq 2 \end{cases}$

5.20. $f(x) = \begin{cases} x + 1, & x \leq 0 \\ \ln x, & 0 < x \leq 1 \\ e^x, & x > 1 \end{cases}$

5.6. $f(x) = \begin{cases} x + 2, & x < -2 \\ 4 - x^2, & -2 \leq x \leq 1 \\ \frac{3}{x}, & x \geq 2 \end{cases}$

5.21. $f(x) = \begin{cases} -x, & x \leq 0 \\ x, & 0 < x \leq 1 \\ \log_2 x, & x > 1 \end{cases}$

$$5.7. f(x) = \begin{cases} -3 - x, & x < -2 \\ x^2 - 5, & -2 \leq x \leq 2 \\ \frac{2}{x}, & x > 2 \end{cases}$$

$$5.8. f(x) = \begin{cases} 2x, & x < 0 \\ \sin x, & 0 \leq x \leq \pi \\ \pi - x, & x > \pi \end{cases}$$

$$5.9. f(x) = \begin{cases} x^2 + 1, & x \leq 0 \\ \cos x, & 0 < x < \pi \\ -2, & x > \pi \end{cases}$$

$$5.10. f(x) = \begin{cases} x^2 + 2, & x \leq 0 \\ e^x, & 0 < x < 2 \\ x - 3, & x \geq 2 \end{cases}$$

$$5.11. f(x) = \begin{cases} x + 2, & x \leq -2 \\ x^2 + 4, & -2 < x \leq 2 \\ -3, & x > 2 \end{cases}$$

$$5.12. f(x) = \begin{cases} -x - 1, & x \leq 0 \\ x^2 - 1, & 0 < x \leq 2 \\ 4, & x > 2 \end{cases}$$

$$5.13. f(x) = \begin{cases} 2^{-x}, & x \leq 0 \\ x + 1, & 0 < x \leq 4 \\ 5, & x > 4 \end{cases}$$

$$5.14. f(x) = \begin{cases} 2^x, & x \leq -1 \\ x, & -1 < x \leq 3 \\ -3, & x > 3 \end{cases}$$

$$5.22. f(x) = \begin{cases} x, & x \leq 1 \\ \frac{1}{x}, & 1 < x \leq 2 \\ 0,5; & x > 2 \end{cases}$$

$$5.23. f(x) = \begin{cases} x^2, & x \leq 1 \\ \ln x, & 1 < x \leq e \\ 2, & x > e \end{cases}$$

$$5.24. f(x) = \begin{cases} -x, & x \leq 0 \\ \operatorname{tg} x, & 0 < x < \frac{\pi}{4} \\ 1, & x \geq \frac{\pi}{4} \end{cases}$$

$$5.25. f(x) = \begin{cases} x + 2, & x \leq -1 \\ x^2, & -1 < x \leq 1 \\ \frac{-2}{x}, & x > 1 \end{cases}$$

$$5.26. f(x) = \begin{cases} -x^2 + 1, & x \leq 0 \\ \cos x, & 0 < x \leq \frac{\pi}{2} \\ x - \frac{\pi}{2}, & x > \frac{\pi}{2} \end{cases}$$

$$5.27. f(x) = \begin{cases} 2^x, & x \leq 0 \\ x, & 0 < x \leq 2 \\ 2, & x > 2 \end{cases}$$

$$5.28. f(x) = \begin{cases} \ln(-x), & x < 0 \\ \sin x, & 0 \leq x \leq \pi \\ x - \frac{\pi}{2}, & x > \pi \end{cases}$$

$$5.29. f(x) = \begin{cases} x^3, & x \leq 0 \\ x, & 0 < x \leq 1 \\ \frac{1}{x}, & x > 1 \end{cases}$$

$$5.15. f(x) = \begin{cases} -x^2, & x \leq 0 \\ \sin x, & 0 < x \leq \frac{\pi}{2} \\ 1, & x \geq \frac{\pi}{2} \end{cases}$$

$$5.30. f(x) = \begin{cases} \left(\frac{1}{2}\right)^x, & x \leq 0 \\ x + \frac{1}{2}, & 0 < x \leq 2 \\ 2, & x > 2 \end{cases}$$

Задание 6. Найти частное двух комплексных чисел. Полученное число представить в тригонометрической и показательной формах записи и изобразить на комплексной плоскости.

$$6.1. z = \frac{i}{i+1}.$$

$$6.2. z = \frac{1+i\sqrt{3}}{1-i\sqrt{3}}.$$

$$6.3. z = \frac{2i}{i-\sqrt{3}}.$$

$$6.4. z = \frac{\sqrt{3}-i}{\sqrt{3}+i}.$$

$$6.5. z = \frac{-1+i}{i}.$$

$$6.6. z = \frac{3-i\sqrt{3}}{5i}.$$

$$6.7. z = \frac{13}{\sqrt{6}-i\sqrt{2}}.$$

$$6.8. z = \frac{5i}{1-i}.$$

$$6.9. z = \frac{-\sqrt{3}+i}{-\sqrt{3}-i}.$$

$$6.16. z = \frac{1-i\sqrt{3}}{i}.$$

$$6.17. z = \frac{6}{1+i}.$$

$$6.18. z = \frac{1-i\sqrt{3}}{3i}.$$

$$6.19. z = \frac{7}{\sqrt{2}+i\sqrt{6}}.$$

$$6.20. z = \frac{3i}{\sqrt{3}+i}.$$

$$6.21. z = \frac{-\sqrt{5}+i\sqrt{5}}{-6i}.$$

$$6.22. z = \frac{\frac{1}{2}+i}{3+i}.$$

$$6.23. z = \frac{7+i7}{-3i}.$$

$$6.24. z = \frac{11}{-2\sqrt{3}+i2}.$$

$$6.10. z = \frac{3+i}{-2+i}.$$

$$6.11. z = \frac{\sqrt{3}+3i}{-4i}.$$

$$6.12. z = \frac{-5}{\sqrt{11}-i\sqrt{11}}.$$

$$6.13. z = \frac{-i}{\sqrt{3}i+1}.$$

$$6.14. z = \frac{3}{-\sqrt{13}+i\sqrt{13}}.$$

$$6.15. z = \frac{2\sqrt{2}-i2\sqrt{2}}{3i}.$$

$$6.25. z = \frac{2i}{\sqrt{3}i-1}.$$

$$6.26. z = \frac{-1-i\sqrt{3}}{-1+i\sqrt{3}}.$$

$$6.27. z = \frac{-3-i}{2-i}.$$

$$6.28. z = \frac{2\sqrt{3}-i}{5i}.$$

$$6.29. z = \frac{-2i}{\sqrt{3}-i}.$$

$$6.30. z = \frac{4i}{1-i\sqrt{3}}.$$

Задание 7. Вычислить двумя способами:

- 1) по формуле Муавра;
- 2) в алгебраической форме.

$$7.1. (-\sqrt{3}+i)^5.$$

$$7.2. (-2-i2\sqrt{3})^3.$$

$$7.3. (\sqrt{5}-i\sqrt{5})^4.$$

$$7.4. (-\sqrt{11}+i\sqrt{11})^6.$$

$$7.5. (1+i)^7.$$

$$7.6. \left(-\frac{\sqrt{3}}{2}-i\frac{1}{2}\right)^4.$$

$$7.7. (\sqrt{15}-i\sqrt{5})^6.$$

$$7.16. \left(\frac{1}{2}-i\frac{\sqrt{3}}{2}\right)^4.$$

$$7.17. (-1+i\sqrt{3})^6.$$

$$7.18. \left(-\frac{1}{2}+i\frac{\sqrt{3}}{2}\right)^5.$$

$$7.19. (2\sqrt{3}-2i)^3.$$

$$7.20. (1-i\sqrt{3})^5.$$

$$7.21. (-\sqrt{7}+i\sqrt{21})^3.$$

$$7.22. (-8+8\sqrt{3}i)^5.$$

$$7.8. (\sqrt{2} - i\sqrt{2})^6.$$

$$7.9. \left(\frac{\sqrt{3}}{5} - \frac{i}{5}\right)^3.$$

$$7.10. \left(-\frac{\sqrt{3}}{4} - \frac{i}{4}\right)^4.$$

$$7.11. (-\sqrt{6}i - \sqrt{6})^4.$$

$$7.12. (-\sqrt{2}i + \sqrt{2})^6.$$

$$7.13. (\sqrt{12} + i\sqrt{12})^5.$$

$$7.14. \left(\frac{\sqrt{3}}{3} - \frac{i}{3}\right)^4.$$

$$7.15. (-\sqrt{3} + i3)^5.$$

$$7.23. (-3 + i\sqrt{3})^4.$$

$$7.24. (\sqrt{3} - i\sqrt{3})^7.$$

$$7.25. \left(-\frac{2}{3}i + \frac{2}{3}\right)^5.$$

$$7.26. \left(-\frac{1}{7} + \frac{i\sqrt{3}}{7}\right)^3.$$

$$7.27. (-5\sqrt{3} - 5i)^4.$$

$$7.28. (2 - i2\sqrt{3})^3.$$

$$7.29. (-i + 1)^7.$$

$$7.30. (-\sqrt{5} - \sqrt{5}i)^6.$$

Задание 8. Найти все значения корня и изобразить их на комплексной плоскости.

$$8.1. \sqrt[3]{8}.$$

$$8.2. \sqrt[4]{-\frac{1}{16}}.$$

$$8.3. \sqrt[4]{-1}.$$

$$8.4. \sqrt[3]{-\frac{1}{8}}.$$

$$8.5. \sqrt[4]{2 - i2}.$$

$$8.6. \sqrt[4]{-27}.$$

$$8.7. \sqrt[4]{-16}.$$

$$8.16. \sqrt[4]{\frac{-1 - i\sqrt{3}}{2}}.$$

$$8.17. \sqrt[3]{\frac{i}{27}}.$$

$$8.18. \sqrt[5]{-i}.$$

$$8.19. \sqrt[3]{-i \cdot 27}.$$

$$8.20. \sqrt[3]{-2 - i2\sqrt{3}}.$$

$$8.21. \sqrt[5]{-32i}.$$

$$8.22. \sqrt[5]{i}.$$

$$8.8. \sqrt[4]{-\frac{1}{81}}.$$

$$8.23. \sqrt[3]{3 - i\sqrt{3}}.$$

$$8.9. \sqrt[4]{-\frac{1}{2} + i\frac{\sqrt{3}}{2}}.$$

$$8.24. \sqrt[4]{-81 + i81\sqrt{3}}.$$

$$8.10. \sqrt[4]{-128 + i128\sqrt{3}}.$$

$$8.25. \sqrt[4]{8 - i8\sqrt{3}}.$$

$$8.11. \sqrt[5]{-32i}.$$

$$8.26. \sqrt[4]{1}.$$

$$8.12. \sqrt[3]{-\frac{i}{125}}.$$

$$8.27. \sqrt[4]{-\frac{1}{2} + i\frac{\sqrt{3}}{2}}.$$

$$8.13. \sqrt[5]{-32 + i32}.$$

$$8.28. \sqrt[4]{-8 + i8\sqrt{3}}.$$

$$8.14. \sqrt[5]{-1+i}.$$

$$8.29. \sqrt[5]{4\sqrt{2} - i4\sqrt{2}}.$$

$$8.15. \sqrt[4]{-\frac{1}{32} + i\frac{\sqrt{3}}{32}}.$$

$$8.30. \sqrt[4]{-128 - i128\sqrt{3}}.$$

Задание 9. Решить уравнения, выполнить проверку.

$$9.1. z^2 + (3i - 2)z + 5 - 3i = 0.$$

$$9.2. z^2 - (2i - 5)z + 5 - 5i = 0.$$

$$9.3. z^2 - (1 + 3i)z - 1 + \frac{3}{2}i = 0.$$

$$9.4. z^2 + (3i - 2)z + 1 - 3i = 0.$$

$$9.5. iz^2 + (1 + i)z + 4i + \frac{1}{2} = 0.$$

$$9.6. z^2 + (1 - i)z - \frac{1}{2}i + 4 = 0.$$

$$9.7. z^2 - (2 + i)z + \frac{3}{4} + i = 0.$$

$$9.8. -iz^2 + (2 - i)z + 1 + 3i = 0.$$

$$\mathbf{9.9.} z^2 + (2i+1)z + \left(i + \frac{3}{2}\right) = 0.$$

$$\mathbf{9.10.} z^2 - \left(\frac{1}{2}i - 2\right)z + \left(-\frac{1}{2}i - \frac{1}{16}\right) = 0.$$

$$\mathbf{9.11.} 2iz^2 + (i-3)z + \left(i - \frac{3}{4}\right) = 0.$$

$$\mathbf{9.12.} -\frac{1}{4}z^2 + (1-3i)z + (6i-1) = 0.$$

$$\mathbf{9.13.} z^2 + (6-i)z + \left(-3i - \frac{1}{4}\right) = 0.$$

$$\mathbf{9.14.} z^2 - (4i+1)z + \left(2i - \frac{3}{2}\right) = 0.$$

$$\mathbf{9.15.} -iz^2 + \left(2i - \frac{1}{2}\right)z + \left(\frac{1}{16}i + \frac{1}{2}\right) = 0.$$

$$\mathbf{9.16.} \left(-6 + \frac{5}{2}i\right)z^2 + (5i+1)z + 1 = 0.$$

$$\mathbf{9.17.} \frac{1}{4}z^2 + (5i-1)z + (-10i-23) = 0.$$

$$\mathbf{9.18.} z^2 + (2+3i)z + 3i = 0.$$

$$\mathbf{9.19.} z^2 + (2i+1)z + (i-1) = 0.$$

$$\mathbf{9.20.} (-i-1)z^2 + (2i-1)z + 1 = 0.$$

$$\mathbf{9.21.} \left(1 + \frac{1}{4}i\right)z^2 + (3i-1)z - 6 = 0.$$

$$\mathbf{9.22.} (2-i)z^2 + (i-1)z + \frac{1}{2} = 0.$$

$$\mathbf{9.23.} (2-3i)z^2 + (2i-3)z + 1 = 0.$$

$$\mathbf{9.24.} z^2 + (2i+3)z + (1+3i) = 0.$$

$$\mathbf{9.25.} (2i+1)z^2 + (4i-3)z - 3 = 0.$$

9.26. $z^2 + (3i + 4)z + (6i + 1) = 0.$

9.27. $(i - 1)z^2 + (2i - 5)z - 5 = 0.$

9.28. $(i - 3)z^2 + (2i - 4)z - 1 = 0.$

9.29. $\frac{5}{2}z^2 + (i - 5)z + (1 - i) = 0.$

9.30. $z^2 + (i - 2)z + (4 - i) = 0.$

Задание 10. Изобразить заданную область.

10.1. $|z - 1| \leq 1, |z + 1| > 2.$

10.2. $|z - 1 - i| \geq 1, 0 \leq \operatorname{Re} z < 2, 0 < \operatorname{Im} z \leq 2.$

10.3. $|z - 1 - i| < 1, |\arg z| \leq \frac{\pi}{4}.$

10.4. $|z| \leq 1, \arg(z + i) > \frac{\pi}{4}.$

10.5. $|z + i| \leq 3, |z - i| > 3.$

10.6. $|z + i| \geq 1, |z| \leq 2.$

10.7. $|z + i| < 2, 0 < \operatorname{Re} z \leq 1.$

10.8. $1 \leq |z - 1| \leq 2, \operatorname{Im} z \geq 0, \operatorname{Re} z < 1.$

10.9. $1 \leq |z - i| < 2, \operatorname{Re} z \leq 0, \operatorname{Im} z > 1.$

10.10. $|z| < 2, \operatorname{Re} z \geq 1, \arg z < \frac{\pi}{4}.$

10.11. $|z| > 1, -1 < \operatorname{Im} z \leq 1, 0 < \operatorname{Re} z \leq 2.$

10.12. $|z - 1| > 1, -1 \leq \operatorname{Im} z < 0, 0 \leq \operatorname{Re} z < 3.$

10.13. $|z + i| < 1, -\frac{3\pi}{4} \leq \arg z \leq -\frac{\pi}{4}.$

10.14. $|z - i| \leq 1, -\frac{\pi}{2} < \arg(z - i) < \frac{\pi}{4}.$

10.15. $|z + 1| \geq 1, |z + i| < 1.$

- 10.16.** $|z + i| \geq 1$, $|z| \leq 3$.
- 10.17.** $|z - 1 + i| \geq 1$, $\operatorname{Re} z < 1$, $\operatorname{Im} z \leq -1$.
- 10.18.** $|z - 1 - i| \leq 1$, $\operatorname{Im} z > 1$, $\operatorname{Re} z \geq 1$.
- 10.19.** $|z - i| \leq 2$, $\operatorname{Re} z > 1$.
- 10.20.** $|z + i| \leq 2$, $|z - i| > 2$.
- 10.21.** $|z - 2 - i| \leq 2$, $\operatorname{Re} z \geq 3$, $\operatorname{Im} z < 1$.
- 10.22.** $|\operatorname{Re} z| \leq 1$, $|\operatorname{Im} z| < 2$.
- 10.23.** $|z - 2 - i| \geq 1$, $1 \leq \operatorname{Re} z < 3$, $0 < \operatorname{Im} z \leq 3$.
- 10.24.** $|z - i| < 1$, $|\arg z| \geq \frac{\pi}{4}$.
- 10.25.** $|z - 1| < 1$, $\arg z \leq \frac{\pi}{4}$, $\arg(z - 1) > \frac{\pi}{4}$.
- 10.26.** $1 < z \cdot \bar{z} < 2$, $\operatorname{Re} z > 0$, $0 \leq \operatorname{Im} z \leq 1$.
- 10.27.** $z \cdot \bar{z} \leq 2$, $\operatorname{Re} z < 1$, $\operatorname{Im} z > -1$.
- 10.28.** $z \cdot \bar{z} < 2$, $\operatorname{Re} z \leq 1$, $\operatorname{Im} z > -1$.
- 10.29.** $|z| > 2$, $-2 < \operatorname{Im} z \leq 2$, $0 < \operatorname{Re} z \leq 3$.
- 10.30.** $|z - 3i| \geq 1$, $0 < \operatorname{Im} z \leq 3$, $-1 < \operatorname{Re} z < 1$.